

# **Cambridge O Level**

| CANDIDATE<br>NAME                      |  |                     |
|--|--|---------------------|
| CENTRE<br>NUMBER                       |  | CANDIDATE<br>NUMBER |
| ADDITIONAL MATHEMATICS 4037/22         |  |                     |
| Paper 2                                |  | May/June 2022       |
|  |  | 2 hours             |
| You must answer on the question paper. |  |                     |

No additional materials are needed.

#### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].



## Mathematical Formulae

### 1. ALGEBRA

# Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Binomial Theorem** 

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ 

Arithmetic series 
$$u_n = a + (n-1)d$$
  
 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$ 

Geometric series

$$u_{n} = ar^{n-1}$$

$$S_{n} = \frac{a(1-r^{n})}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

#### **2. TRIGONOMETRY**

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for  $\triangle ABC$ 

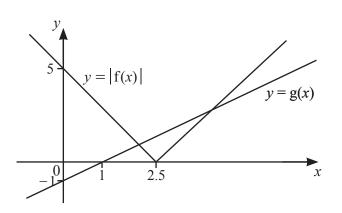
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc\cos A$$
$$\Delta = \frac{1}{2}bc\sin A$$

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## 1 DO NOT USE A CALCULATOR IN THIS QUESTION.

A curve has equation  $y = \frac{6 + \sqrt{x}}{3 + \sqrt{x}}$  where  $x \ge 0$ . Find the exact value of y when x = 6. Give your answer in the form  $a + b\sqrt{c}$ , where a, b and c are integers. [3]

3



The diagram shows the graphs of y = |f(x)| and y = g(x), where y = f(x) and y = g(x) are straight lines. Solve the inequality  $|f(x)| \le g(x)$ . [5]

3 Find the possible values of k for which the equation  $kx^2 + (k+5)x - 4 = 0$  has real roots. [5]

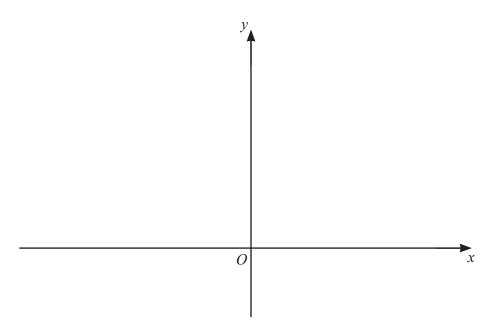
4 Variables x and y are related by the equation  $y = 1 + \frac{2}{x} + \frac{1}{x^2}$  where x > 0. Use differentiation to find the approximate change in x when y increases from 4 by the small amount 0.01. [5]

4037/22/M/J/22

5 (a) Solve the equation 
$$\frac{625^{\frac{x^3-1}{2}}}{125^{x^3}} = 5.$$
 [3]

5

(b) On the axes, sketch the graph of  $y = 4e^x + 3$  showing the values of any intercepts with the coordinate axes. [2]



6 (a) In this question, i is a unit vector due east and j is a unit vector due north.

A cyclist rides at a speed of  $4 \text{ ms}^{-1}$  on a bearing of 015°. Write the velocity vector of the cyclist in the form  $x\mathbf{i} + y\mathbf{j}$ , where x and y are constants. [2]

(b) A vector of magnitude 6 on a bearing of 300° is added to a vector of magnitude 2 on a bearing of 230° to give a vector v. Find the magnitude and bearing of v. [5]

7 Differentiate  $y = \frac{e^{4x} \tan x}{\ln x}$  with respect to x.

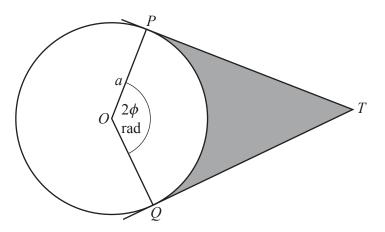
7

[4]

- 8 The function f is defined by  $f(x) = 3\sin^2 x 2\cos x$  for  $2 \le x \le 4$ , where x is in radians.
  - (a) Find the *x*-coordinate of the stationary point on the curve y = f(x). [5]

(b) Solve the equation  $f(x) = 1 - 3\cos x$ .

- 10
- 9 In this question all lengths are in centimetres.



The diagram shows a circle, centre *O*, radius *a*. The lines *PT* and *QT* are tangents to the circle at *P* and *Q* respectively. Angle *POQ* is  $2\phi$  radians.

(a) In the case when the area of the sector *OPQ* is equal to the area of the shaded region, show that  $\tan \phi = 2\phi$ . [4]

(b) In the case when the perimeter of the sector OPQ is equal to half the perimeter of the shaded region, find an expression for  $\tan \phi$  in terms of  $\phi$ . [3]

- 10 (a) A geometric progression has first term a and common ratio r, where r > 0. The second term of this progression is 8. The sum of the third and fourth terms is 160.
  - (i) Show that *r* satisfies the equation  $r^2 + r 20 = 0$ . [4]

(ii) Find the value of *a*.

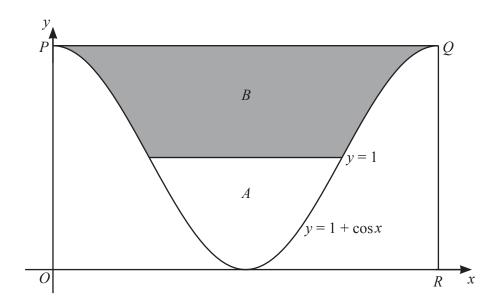
[3]

(b) An arithmetic progression has first term p and common difference 2. The qth term of this progression is 14.A different arithmetic progression has first term p and common difference 4. The sum of the first q terms of this progression is 168.

13

Find the values of p and q.

[6]



The diagram shows part of the line y = 1 and one complete period of the curve  $y = 1 + \cos x$ , where *x* is in radians. The line *PQ* is a tangent to the curve at *P* and at *Q*. The line *QR* is parallel to the *y*-axis. Area *A* is enclosed by the line y = 1 and the curve. Area *B* is enclosed by the line y = 1, the line *PQ* and the curve.

Given that area A: area B is 1: k find the exact value of k.

[9]

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11

14

Continuation of working space for Question 11.

# Question 12 is printed on the next page.

12 A curve is such that  $\frac{d^2y}{dx^2} = \left(\frac{\sqrt{x}+1}{\sqrt[4]{x}}\right)^2$ . Given that the gradient of the curve is  $\frac{4}{3}$  at the point (1, -1), find the equation of the curve. [7]

16

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